CRYOSPHERE: SINGLE-PARTICLE HETEROGENEOUS RECONSTRUCTION FROM CRYO EM

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Paper under double-blind review

Abstract

The three-dimensional structure of proteins plays a crucial role in determining their function. Protein structure prediction methods, like AlphaFold, offer rapid access to a protein's structure. However, large protein complexes cannot be reliably predicted, and proteins are dynamic, making it important to resolve their full conformational distribution. Single-particle cryo-electron microscopy (cryo-EM) is a powerful tool for determining the structures of large protein complexes. Importantly, the numerous images of a given protein contain underutilized information about conformational heterogeneity. These images are very noisy projections of the protein, and traditional methods for cryo-EM reconstruction are limited to recovering only one or a few consensus conformations. In this paper, we introduce cryoSPHERE, which is a deep learning method that uses a nominal protein structure (e.g., from AlphaFold) as input, learns how to divide it into segments, and moves these segments as approximately rigid bodies to fit the different conformations present in the cryo-EM dataset. This approach provides enough constraints to enable meaningful reconstructions of single protein structural ensembles. We demonstrate this with two synthetic datasets featuring varying levels of noise, as well as one real dataset. We show that cryoSPHERE is very resilient to the high levels of noise typically encountered in experiments, where we see consistent improvements over the current state-of-the-art for heterogeneous reconstruction.

1 INTRODUCTION

Single-particle cryo-electron microscopy (cryo-EM) is a powerful technique for determining the 033 three-dimensional structure of biological macromolecules, including proteins. In a cryo-EM exper-034 iment, millions of copies of the same protein are first frozen in a thin layer of vitreous ice and then imaged using an electron microscope. This yields a micrograph: a noisy image containing 2D projections of individual proteins. The protein projections are then located on this micrograph and cut out so that an experiment typically yields 10^4 to 10^7 images of size $N_{\text{pix}} \times N_{\text{pix}}$ of individual pro-037 teins, referred to as particles. Our goal is to reconstruct the possible structures of the proteins given these images. Frequently, proteins are conformationally heterogeneous and each copy represents a different structure. Conventionally, this information has been discarded, and all of the sampled 040 structures were assumed to be in only one or a few conformations (homogeneous reconstruction). 041 Here, we would like to recover all of the structures in a *heterogeneous* reconstruction. 042

Structure reconstruction from cryo-EM presents a number of challenges. First, each image shows a 043 particle in a different, unknown orientation. Second, because of the way the electrons interact with 044 the protein, the spectrum of the images is flipped and reduced. Mathematically, this corresponds to a convolution of each individual image with the Point Spread Function (PSF). Third, the images typi-046 cally have a very low signal-to-noise ratio (SNR). For these reasons, it is very challenging to perform 047 de novo cryo-EM reconstruction. Standard methods, produce electron densities averaged over many, 048 if not all conformations (Scheres, 2012; Punjani et al., 2017), performing discrete heterogeneous reconstruction. More recent methods attempt to extract continuous conformational heterogeneity, e.g., by imposing constraints on the problem through an underlying structure deformed to fit the differ-051 ent conformations present in the dataset, see e.g. Rosenbaum et al. (2021); Zhong et al. (2021b); Li et al. (2023). AlphaFold (Jumper et al., 2021) and RosettaFold (Baek et al., 2021) can provide 052 such a structure based on the primary sequence of the protein only. In spite of this strong prior, it is still difficult to recover meaningful conformations. The amount of noise and the fact that we



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091 092 Figure 1: Flow chart of our network. The learnable parts of the model are the encoder, the decoder and the Gaussian mixture. Note that even though the transformations predicted by the decoder are on a per image basis, that is not the case of the Gaussian mixture, which is shared across all particles.

observe only 2D projections creates local minima that are difficult to escape (Zhong et al., 2021b;
 Rosenbaum et al., 2021), leading to unrealistic conformations.

To remedy this, we root our method in the observation that different conformations can often be explained by large scale movements of domains of the protein (Mardt et al., 2022). Specifically, we develop a variational auto-encoder (VAE) (Kingma & Welling, 2014) that, from a nominal structure and a set of cryo-EM images:

- Learns how to divide the amino-acid chain into segments, given a user defined maximum number of segments; see Figure 2. The nominal structure can for instance be obtained by AlphaFold (Jumper et al., 2021).
- For each image, learns approximately rigid transformations of the identified segments of the nominal structure, which effectively allows us to recover different conformations on an image-by-image (single particle) basis.

These two steps happen concurrently, and the model is end-to-end differentiable. The model is illustrated in Figure 1. The implementation of the model is available on github 1 .

Note that what we call a segment is conceptually different from a domain in the structural biology sense. The domains of a protein play a pivotal role in diverse functions, engaging in interactions with other proteins, DNA/RNA, or ligand, while also serving as catalytic sites that contribute significantly to the overall functionality of the protein, see e.g. Schulz & Schirmer (1979); Nelson et al. (2017).
By comparison, the segments we learn do not necessarily have a biological function. However, while not strictly necessary for the function of the method, experiments in Section 5 show that our VAE often recovered the actual domains corresponding to different conformations.

2 NOTATIONS AND PROBLEM FORMULATION

In what follows, we consider only the C_{α} atoms of the protein. A protein made of a number $R_{\text{res}} \in \mathbb{N}^*$ of residues r_i is denoted $S = \{r_i\}_{i=1}^{R_{\text{res}}}$, where the coordinates of residue *i* are the coordinates of its C_{α} atom. The electron density map of a structure *S*, also called a volume, is a function $V_S : \mathbb{R}^3 \to \mathbb{R}$, where $V_S(x)$ is proportional to the probability density function of an electron of *S* being present in an infinitesimal region around $x \in \mathbb{R}^3$. That is, the expected number of electrons in $B \subseteq \mathbb{R}^3$ is proportional to $\int_B V_S(x) dx$.

Assume we have a set of 2D images $\{I_i\}_{i=1}^N$ of size $N_{\text{pix}} \times N_{\text{pix}}$, representing 2D projections of different copies of the same protein in different conformations. Traditionally, the goal of cryo-EM heterogeneous reconstruction has been to recover, for each image i, the electron density map V_i corresponding to the underlying conformation present in image i; see Section 4 for a review of these methods. However, following recent works, e.g., Rosenbaum et al. (2021); Zhong et al. (2021b), we aim at recovering, for each image i, the underlying structure S_i explaining the image. That is, we try to recover the precise position in \mathbb{R}^3 of each residue.

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¹⁰⁸ 3 METHOD – CRYOSPHERE

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110 In this section, we present our method for single-particle heterogeneous reconstruction, denoted 111 cryoSPHERE. The method focuses on structure instead of volume reconstruction. It differs from 112 the previous (Rosenbaum et al., 2021) and concurrent (Li et al., 2023) works along this line in 113 the way the movements of the residues are constrained: instead of deforming the base structure 114 on a residue level and then imposing a loss on the reconstructed structure, our method learns to decompose the amino-acid chain of the protein into segments and, for each image I_i , to rigidly 115 move the learnt segments of a base structure S_0 to match the conformation present in that image. 116 This is motivated by the fact that different conformations of large proteins often can be explained by 117 large scale movements of its domains (Mardt et al., 2022). 118

The base structure S_0 can be obtained using methods like AlphaFold (Jumper et al., 2021) and RosettaFold (Baek et al., 2021), based on the amino-acid sequence of the protein. In Section 5, we further fit the AlphaFold predicted structure into a volume recovered by a custom backprojection algorithm provided by Zhong et al. (2020).

We use a type of VAE architecture, see Figure 1. We map each image to a latent variable by a stochastic encoder, which is then decoded to a rigid body transformation per segment. Based on these transformations and the segment decomposition, the underlying structure S_0 is deformed, posed and turned into a volume that is used to create a projected image. This image is then compared to the input image. After that, the backward pass updates the parameters of the encoder, decoder and Gaussian mixture. We now describe the details of our model.

130 3.1 IMAGE FORMATION MODEL

To compute the 2D projection of the protein structure S, we first estimate its 3D electron density map V:

$$V_S(r) := \sum_{a \in S} A_a \exp\left(-\frac{||r-a||^2}{2\sigma^2}\right) \tag{1}$$

136 where A_a is the average number of electrons per atom in residue $a, r \in \mathbb{R}^3$ and $\sigma = 2$ by default. 137 Hence, the protein's electron density is approximated as the sum of Gaussian kernels centered on its 138 C_{α} atoms. From these density maps, we then compute an image projection $I \in \mathbb{R}^{N_{\text{pix}} \times N_{\text{pix}}}$ as:

$$I(R,t,S)(r_x,r_y) = g * \int_{\mathbb{R}} V_{RS+t}(r) dr_z,$$
(2)

where $(r_x, r_y) \in \mathbb{R}^2$ are the coordinates of a pixel, $r_z \in \mathbb{R}$ is the coordinate along the z axis, $R \in SO(3)$ is a rotation matrix and $t \in \mathbb{R}^3$ is a translation vector. The abuse of notation RS + tmeans that every atom of S is rotated according to R and then translated according to t. The image is finally convolved with the point spread function (PSF) g, which in Fourier space is the contrast transfer function (CTF), see Vulović et al. (2013). Note that the integral can be computed exactly for our choice of approximating the density map as a sum of Gaussian kernels, which significantly reduces the computing time.

149 3.2 MAXIMUM LIKELIHOOD WITH VARIATIONAL INFERENCE

To learn a distribution of the different conformations, we hypothesize that the conformation seen in image I_i depends on a latent variable $z_i \in \mathbb{R}^L$, with prior $p(z_i)$. Let $f_{\theta}(S_0, z)$ be a function which, for a given base structure S_0 and latent variable z, outputs a new transformed structure S. This function depends on a set of learnable parameters θ . Then, the conditional likelihood of an image $I^* \in \mathbb{R}^{N_{\text{pix}} \times N_{\text{pix}}}$ with a pose given by a rotation matrix R and a translation vector t is modeled as $p_{\theta}(I^*|R, t, S_0, z) = \mathcal{N}(I^*|I(R, t, f_{\theta}(S_0, z)), \sigma^2_{\text{noise}})$, where σ^2_{noise} is the variance of the observation noise. The marginal likelihood is thus given by

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$$p_{\theta}(I^{\star}|R, t, S_0) = \int p_{\theta}(I^{\star}|R, t, S_0, z) p(z) dz.$$
(3)

160 In practice, the pose (R, t) of a given image is unknown. However, following similar works (Zhong 161 et al., 2021b; Li et al., 2023), we suppose that we can estimate R and t to sufficient accuracy using off-the-shelf methods (Scheres, 2012; Punjani et al., 2017). 162 Directly maximizing the likelihood (3) is infeasible because one needs to marginalize over the la-163 tent variable. For this reason, we adopt the VAE framework, conducting variational inference on 164 $p_{\theta}(z|I^*) \propto p_{\theta}(I^*|z)p(z)$, and simultaneously performing maximum likelihood estimation on the 165 parameters θ .

Let $q_{\psi}(z|I^*)$ denote an approximate posterior distribution over the latent variables. We can then maximize the evidence lower-bound (ELBO):

$$\mathcal{L}(\theta, \psi) = \mathbb{E}_{q_{\psi}}[\log p_{\theta}(I^{\star}|z)] - \mathcal{D}_{\mathrm{KL}}(q_{\psi}(z|I^{\star})||p(z))$$
(4)

which lower bounds the log-likelihood $\log p_{\theta}(I^*)$. Here D_{KL} denotes the Kullback-Leibler (KL) divergence. In this framework f_{θ} is called the decoder and $q_{\psi}(z|I^*)$ the encoder.

173 174 3.3 SEGMENT DECOMPOSITION

To handle the often very low SNR encountered in cryo-EM data, we regularize the transformation of the structure produced by the decoder by restricting it to transforming whole segments of the protein. We fix a maximum number of segments $N_{\text{segm}} \in \{1, ..., R_{\text{res}}\}$ and we represent the decomposition of the protein by a stochastic matrix $G \in \mathbb{R}^{R_{\text{res}} \times N_{\text{segm}}}$. The rows of G represent "how much of each residue belongs to each segment", and our objective is to ensure that each residue *primarily* belongs to one segment, that is:

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$$\forall i \in \{1, \dots, R_{\text{res}}\}, \exists m^{\star} \in \{1, \dots, N_{\text{segm}}\}$$

s.t $\sum_{m \neq m^{\star}} G_{im} \ll 1$ (5)

We also aim for the segments to respect the sequential structure of the amino acid chain, and the model to be end-to-end differentiable. Without end-to-end differentiability, we could not apply the reparameterization trick and we would have to resort to Monte Carlo estimation of the gradient of the segments, which has a higher variance, see e.g. Mohamed et al. (2019).

To meet these criteria, we fit a Gaussian mixture model (GMM) with N_{segm} components on the real line supporting the residue indices. Each component m has a mean μ_m , standard deviation σ_m and a logit weight α_m . The $\{\alpha_m\}$ are passed into a softmax to obtain the weights $\{\pi_m\}$ of the GMM, ensuring they are positive and summing to one. We further anneal the Gaussian components by a temperature $\tau > 0$, and define the probability that a residue *i* belongs to segment *m* as:

$$G_{im} := \frac{\{\phi(i|\mu_m, \sigma_m^2)\pi_m)\}^{\tau}}{\sum_{k=1}^{N_{\text{segm}}} \{\phi(i|\mu_k, \sigma_k^2)\pi_k\}^{\tau}}$$
(6)

where $\phi(x|\mu, \sigma^2)$ is the unidimensional Gaussian probability density function with mean μ and variance σ^2 and τ is a fixed hyperparameter. If τ is sufficiently large, we can expect condition (5) to be verified. See Figure 2 for an example of a segment decomposition using a Gaussian mixture.

In this "soft" decomposition of the protein, each residue can belong to more than one segment, allowing for smooth deformations. In addition, the differentiable architecture is amenable to gradient descent methods, and a well chosen τ can approximate a "hard" decomposition of the protein. We set $\tau = 20$ in the experiment section. In our experience, this segmentation procedure is very robust to different initialization and converges in only a few epochs.

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3.4 DECODER ARCHITECTURE

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The decoder describes the distribution of the images given the latent variables, which include:

- 1. One latent variable $z_i \in \mathbb{R}^L$ per image, parameterizing the conformation.
- 2. The global parameters $\{\mu_m, \sigma_m, \alpha_m\}_{m=1}^{N_{\text{segm}}}$ of the GMM describing the segment decomposition.

Figure 2: Example of segments recovered with a Gaussian mixture of 6 components.

Given these latent variables and a base structure S_0 , we parameterize the decoder f_{θ} in three steps. First, a neural network with parameters θ maps $z_i \in \mathbb{R}^L$ to a set of rigid

body transformations, one for each segment $m = 1, ..., N_{\text{segm}}$. The transformation of segment m is represented by a translation vector \vec{t}_m and a unit quaternion \vec{q}_m (Vicci, 2001), which can further be decomposed into an axis of rotation $\vec{\phi}_m$ and rotation angle δ_m . Second, given the parameters of the GMM, we compute the matrix G. Finally, for each residue i of S_0 , we update the coordinates of all its atoms $\{a_{ik}\}_{k=1}^{A_i}$:

1. First, a_{ik} is successively rotated around the axis ϕ_m with an angle $G_{im}\delta_m$ for $m \in \{1, \ldots, N_{\text{segm}}\}$ to obtain updated coordinates a'_{ik} .

2. Second, it is translated according to:
$$a_{ik}'' = a_{ik}' + \sum_{j=m}^{N} G_{im} \vec{t}_m$$
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This way, the transformation for a residue incorporate contributions from all segments, proportionally on how much they belong to the segments. If condition (5) is met, a roughly rigid motion for each segment can be expected.

243 3.5 ENCODER AND PRIORS

244 We follow the classical VAE frame-245 The distribution $q_{\psi}(y|I^{\star})$ work. 246 is given by a normal distribution 247 $\mathcal{N}(\mu(I^{\star}), \operatorname{diag}(\sigma^2(I^{\star})))$ where $\mu \in \mathbb{R}^L$ 248 and $\sigma \in \mathbb{R}^L_{\perp}$ are generated by a neural 249 network with parameters ψ , taking an 250 image I^* as input. Additionally, the approximate posterior distribution on the 251 parameters of the GMM is chosen to be 252 Gaussian and independent of the input 253 image: 254



$$\alpha_m \sim \mathcal{N}(\nu_{\alpha_m}, \beta_{\alpha_m}^2)$$



Figure 3: MD dataset SNR 0.001. Left: Histograms of the distances of the two upper domains. The true distances are in green. The recovered distances are in blue. Right: Predicted against true distances in Ångström. The black line represent x = y. The correlation between the predicted and true distances is 0.73. For the same plot for cryoStar, see Appendix B.2 of the supplementary file.

where $\{\nu_{\mu_m}, \beta_{\mu_m}, \nu_{\sigma_m}, \beta_{\sigma_m}, \nu_{\alpha_m}, \beta_{\alpha_m}\}_{m=1}^{N_{\text{segm}}}$ are parameters that are directly optimized. In practice we use ELU+1 layers for σ_m to avoid negative or null standard deviation.

Finally, we assign standard Gaussian priors to both the local latent variable $z_i \sim \mathcal{N}(0, I_L)$, and the global GMM parameters $\{\mu_m, \sigma_m, \alpha_m, \}_{m=1}^{N_{\text{segm}}}$. This reparameterization (Kingma & Welling, 2014) is straightforward for a Gaussian distribution. Calculating the KL-divergence between two Gaussian distributions as in equation 4, is also straightforward.

267 3.6 Loss

269 Since the images may be preprocessed in unknown ways before running cryoSPHERE, we use a correlation loss between predicted and ground truth image instead of a mean squared error loss,

270 similar to (Li et al., 2023):

$$\mathcal{L}_{corr} = \frac{-I_i^* \cdot I(R_i, t_i, f_{\theta}(S_0, z))}{||I_i^*|| \times ||I(R_i, t_i, f_{\theta}(S_0, z))||}$$
(7)

where \cdot denotes the dot product. The total loss to minimize writes:

$$\mathcal{L}(I, I^{\star}) = \mathcal{L}_{\text{corr}} + \mathcal{D}_{\text{KL}}(q_{\psi}(z|I^{\star})||p(z))$$
(8)

In our experience, it is unnecessary to add any regularization term to the correlation and KL divergence losses, except for datasets featuring a very high degree of heterogeneity. In that case, we offer the option of adding a continuity loss to avoid breaking the protein and a clashing loss to avoid clashing residues, as it is done in (Rosenbaum et al., 2021; Li et al., 2023; Jumper et al., 2021). We describe these losses in Appendix A.1 of the supplementary file.

- 4 RELATED WORKS
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286 Two of the most popular methods for cryo-EM reconstruction, which are not based on deep learning, 287 are RELION (Scheres, 2012) and cryoSPARC (Punjani et al., 2017). Both methods perform volume 288 reconstruction, hypothesize that k conformations are present in the dataset and perform maximum 289 a posteriori estimation over the k density maps, thus performing discrete heterogeneous reconstruction. Both of these algorithms operate in Fourier space using an expectation-maximization algorithm 290 Dempster et al. (1977) and are non-amortized: the poses are refined for each image. Other ap-291 proaches perform continuous heterogeneous reconstruction. For example, 3DVA (Punjani & Fleet, 292 2021b) uses a probabilistic principal component analysis model to learn a latent space. 293

Another class of methods involve deep learning and typically performs continuous heterogeneous reconstruction using a VAE architecture. Of those that attempt to reconstruct a density map, cryo-295 DRGN (Zhong et al., 2020; 2021a) and CryoAI (Levy et al., 2022) use a VAE acting on Fourier space 296 to learn a latent space and a mapping that associates a 3D density map with each latent variable. They 297 perform non-amortized and amortized inference over the poses, respectively. Other methods are de-298 fined in the image space, e.g. 3DFlex (Punjani & Fleet, 2021a) and cryoPoseNet (Nashed et al., 299 2021). They both perform non-amortized inference over the poses. These methods either learn, 300 for a given image I_i , $\{V_i(x_k)\}$ the values at a set of N_{pix}^3 fixed 3D coordinates $\{x_k\}$, representing 301 the volume on a grid (*explicit* parameterization), or they learn an actual function $\hat{V}_i : \mathbb{R}^3 \to \mathbb{R}$ in 302 the form of a neural network that can be queried at chosen coordinates (*implicit* parameterization). 303 These volume-based methods cannot use external structural restraints or force fields as additional 304 information. This limits their applicability to low SNR data sets, which are frequent in protein cryo 305 EM. 306

Other deep learning methods attempt to directly reconstruct structures instead of volumes and share 307 a common process: starting from a plausible base structure, obtained with e.g. AlphaFold (Jumper 308 et al., 2021), for each image, they move each residue of the base structure to fit the conformation 309 present in that specific image. These methods differ on how they parameterize the structure and 310 in the prior they impose on the deformed structure or the motion of the residues. For example 311 AtomVAE (Rosenbaum et al., 2021) considers only residues and penalizes the distances between 312 two subsequent residues that deviate too much from an expected value. CryoFold (Zhong et al., 313 2021b) considers the residue centers and their side-chain and also imposes a loss on the distances 314 between subsequent residues and the distances between the residue centers and their side-chain. 315 Unfortunately, due to the high level of noise and the fact that we observe only projections of the structures, these "per-residue transformation" methods tend to be stuck in local minima, yielding 316 unrealistic conformations unless the base structure is taken from the distribution of conformations 317 present in the images (Zhong et al., 2021b), limiting their applicability on real datasets. Even though 318 AtomVAE (Rosenbaum et al., 2021) could roughly approximate the distribution of states of the 319 protein, it was not able to recover the conformation given a specific image. 320

To reduce the bias that the base structure brings, DynaMight (Schwab et al., 2023) fits pseudo-atoms in a consensus map with a neural network directly. Similar to our work, several other methods constrain the atomic model to rigid body motions. For example e2gmm (Chen & Ludtke, 2021; Chen et al., 2023) deform a nominal structure S_0 based on how much its residues are close to a 324 learnt representation S_{small} of S_0 . This is similar to our GMM, except that their takes place in \mathbb{R}^3 325 and is not used to perform rigid body motion. Instead, they ask the user to define the segmentation 326 in a later step. This is in contrast to cryoSPHERE, which learns the motion and the segmentation 327 concurrently. Using DynaMight (Schwab et al., 2024), Chen et al. (2024) developed a focused 328 refinement on patches of the GMM representation of the protein. These patches are learnt using kmeans on the location of residues and do not depend on the different conformations of the data set. This in contrast to cryoSPHERE where the learning of the segments of the protein is tightly linked 330 to the change of conformation. Concurrently to our work, Li et al. (2023) developed cryoStar which 331 learns to translate each residue independently using a variational auto-encoder. They enforce the 332 local rigidity of the motion of the protein by imposing a similarity loss between the base structure 333 and the deformed structure as well as a clash loss. The interested reader can see Donnat et al. (2022) 334 for an in-depth review of deep learning methods for cryo-EM reconstruction. 335

The reconstruction methods relying on an atomic model, such as cryoStar, DynaMight or cryoSPHERE offer the possibility to the user to provide prior information via this atomic model. They also offer the possibility of deforming the protein according to chemical force fields. This is not the case of the methods performing volume reconstruction without such an atomic model.

5 EXPERIMENTS

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343 In this section, we test cryoSPHERE on a set 344 of synthetic² and real 345 datasets with vary-346 ing level of noise and 347 compare the results to 348 cryoDRGN (Zhong et al., 349 2020) and cryoStar (Li 350 et al., 2023). CryoDRGN 351 is а state-of-the-art 352 method for continuous 353 heterogeneous recon-354 struction, in which the 355 refinement occurs at the 356



Figure 4: MD dataset. Left: cryoSPHERE Recovered segments. The colors denotes different contiguous domains. Middle and right: mean FSC comparison +/- one standard deviation, for cryoSphere and cryoDRGN and cryoStar. For a comparison between cryoStar and cryoDRGN, see Appendix B.2 in the supplementary file.

level of electron densities, while cryoStar is a structural method similar to ours. To our knowledge, the code for AtomVAE and CryoFold is not available and non-trivial to reimplement. For this reason we focus our comparison on the aforementioned methods, which have furthermore reported state-of-the-art performance. In Appendix B.1, we demonstrate that cryoSPHERE is able to recover the exact ground truth when it exists. We also discuss its performances with varying SNR and N_{segm} and show how to debias cryoSPHERE results using DRGN-AI or cryoStar volume method in Appendix B.2. Finally, Appendix B.5 compares the computational costs of cryoSPHERE and cryoStar.

5.1 MOLECULAR DYNAMICS DATASET: BACTERIAL PHYTOCHROME.

366 As a more difficult test case we simulate a continuous motion of a bacterial phytochrome, with PDB 367 entry 4Q0J (Burgie et al., 2014). The trajectory starts at the closed conformation of Figure 11 and 368 ends at the most open conformation on the same figure. It corresponds to a dissociation of the two top parts of the protein. This dataset has a very low SNR of 0.001. Our base structure is obtained by 369 AlphaFold and is subsequently fitted into a homogeneous reconstruction given by the backprojection 370 algorithm. We train cryoSPHERE with $N_{\text{segm}} = 25$, cryoStar, and cryoDRGN for 24 hours each, us-371 ing the same single GPU. We get one predicted structure per image for cryoSPHERE and cryoStar, 372 that we turn into volumes using (1), and one predicted volume per image for cryoDRGN. See Ap-373 pendix B.2 in the supplementary file for details and comparison with different values of N_{segm} . Note 374 that since both cryoSPHERE and cryoStar use a nominal structure, we fit the structure we obtained 375 through AlphaFold in the consensus reconstruction obtained by backprojection and use that exact 376 same structure as the nominal one for both methods.

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²See Appendix B of the supplementary file for details on how we created the synthetic datasets.



Figure 5: EMPIAR10180. Left and middle left: different views of the structures corresponding to the red dots of Figure 48. The motion goes from red (left in the first principal component) to white to blue (right of the principal component). Only the C_{α} atoms are shown. Right and middle right: different views of two volumes recovered by training DRGN-AI on the latent space of cryoSPHERE. The U2 domain disappears on the volume because of a compositional heterogeneity.

390 Figure 3 shows the predicted distance between the two upper parts of the protein being dissociated, 391 against the ground truth distance for each image. In spite of the very low SNR, cryoSPHERE roughly 392 recovers the right distribution of distances. More importantly, the correlation between the predicted 393 distance and ground truth distance is 0.74, showing that cryoSPHERE is able to recover the correct 394 conformation given an image. This is in stark contrast with Rosenbaum et al. (2021) who could not 395 recover the conformation conditionally on an image. In addition, our model has learnt to separate 396 the two mobile top domains from the fix bottom one, as shown by the segment decomposition in Figure 4. Appendix B.2 in the supplementary file shows the same figures for cryoStar. 397

398 We plot the mean of the FSC curves between the predicted volumes and the corresponding ground 399 truth volumes in Figure 4, for cryoSPHERE, cryoDRGN and cryoStar. CryoSPHERE performs 400 better than both cryoDRGN and cryoStar at both the 0.5 and 0.143 cutoffs. We attribute this to three 401 key properties. Firstly, we fit our base structure into a consensus reconstruction. This step corrects the position of the medium-scale elements of the base structure that could have been misplaced, 402 boosting the FSC of cryoSPHERE at the 0.5 cutoff. Secondly, acting directly on the structure level 403 offers a finer resolution than cryoDRGN given the level of noise. Figure 32 shows that cryoDRGN 404 underestimated the opening of the protein and sometimes gives very noisy volumes. That explain 405 why we outperform cryoDRGN at the 0.143 cutoff. Finally, cryoSPHERE is rigidly moving larger 406 segments of the protein. This provide a better resistance to high levels of noise and overfitting 407 compared to moving each residue individually like cryoStar does, providing a possible explanation 408 to the improvement compared to cryoStar at the 0.143 cutoff. 409

- 410 5.2 EMPIAR 10180
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We now demonstrate that cryoSPHERE is applicable to real data as well as large proteins. We run cryoSPHERE on EMPIAR-10180 Plaschka et al. (2017), comprising 327 490 images of a precatalytic spliceosome with 13 941 residues, making it a computationally heavy dataset to tackle. We use the atomic model by Plaschka et al. (2017) (PDB: 5NRL).

Figure 5 shows a set of ten structures taken evenly along the first principal component of the latent space. To interrogate if these structures contain bias from the structural constraints, we perform a volume reconstruction step similar to cryoStar Phase II, see Figure 5.

419 Traversing the first principal component shows that the Sf3b domain gets incurvated down while the 420 helicase move closer to the foot of the protein. This is in line with the literature (Li et al., 2023; 421 Plaschka et al., 2017). The motion of the protein also brings the alpha helix of the Spp381 domain 422 closer to the foot, as corroborated by Li et al. (2023). Comparison between the recovered structures 423 and volumes (Figure 50) shows similar movements, indicating a small amount of bias from the structural constraints. In addition, the absence of density corresponding to the U2 domain in the 424 volume indicates that it there is compositional heterogeneity that cryoSPHERE could not detect, see 425 Figure 5. We provide a movie of the motion and more structures and volumes in appendix B.3 in 426 the supplementary file. 427

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- 429 5.3 EMPIAR-12093
- 431 We now tackle the recently published EMPIAR-12093 (Bódizs et al., 2024). This dataset comprises two sets of images: one non-activated (Pfr) and one activated (Pr). These dataset are very challeng-



Figure 6: EMPIAR12093. Left of the black line: Ten structures sampled along PC1, for cryoSPHERE and cryoStar. Right of the black line: examples of volumes reconstructed by training the cryoStar volume method on the latent space of cryoSPHERE for debiasing. The blue and red volumes correspond to the first and last volumes along PC1. Top row corresponds to Pr; bottom row to Pfr.

ing because of the high level of noise and heterogeneity of the protein, especially in the Pfr dataset. Traditional methods like cryoSparc (Punjani et al., 2017) or cryoDRGN (Zhong et al., 2020; 2021a) fail at reconstructing the upper part of the protein, see Bódizs et al. (2024) and Appendix B.4.

Figure 6 shows principal component 1 traversal for cryoStar and cryoSPHERE. For Pr, both methods are in strong agreement and reveal a rotation of the upper domain around its axis, while the lower part remains stationary. This aligns with previous studies (Wahlgren et al.; Malla et al., 2024)).



467 Figure 7: EMPIAR12093. Distribution of the number of clashes for 2000 randomly chosen structures Pfr dataset, for cryoSPHERE and cryoStar. Two non contiguous residues are said to be clashing if their distance is less than 4 Å.

The Pfr dataset showcases an even lower SNR and more dynamical protein: the protein opens up completely. From consensus reconstructions alone, one could suspect that the upper domains are cut off in the sample preparation procedure. However, the protein is complete in Pr (light-activated) structure and the photocycle is reversible,(Takala et al., 2014) suggesting that this is not the case and that strong conformational heterogeneity that is at play.

For Pfr cryoStar is unable to produce physically plausible results: the top part of the protein appears disordered and shows a random motion. In addition, cryoStar does not recover the "scissoring" motion of protein, which is thought to be active (Bódizs et al., 2024). On the contrary, cryoSPHERE gives a high level of motion in a structured manner and recovers the "scissors" opening of the protein. Without any clashes (Fig. 7). (Bódizs et al., 2024).

Analysis of the dataset on phytochromes illustrates the scope and limitations of the different meth-ods. Pure image-based methods (i.e. cryo DRGN) already fail on the Pr state with its intermediate disorder, while cryoSTAR and cryoSPHERE succeed in obtaining reasonable reconstructions (Fig-ure 6). For the Pfr state it becomes evident that cryoSTAR struggles with the high noise and large motions encoded in the dataset. Its deformation-based approach results in unphysical motions along the first principal component, often leading to structural clashes. In contrast, cryoSPHERE handles the noise effectively, producing physically plausible large-scale motions in both the upper and lower domains, see Figure 7, the supplementary movies and B.4. We assign this superior performance to the higher degree of structural constraints that are used in cryoSPHERE compared to cryoSTAR.

We also performed debiasing of cryoSPHERE with a volume method and show examples of reconstructed volumes in Figure 6. For Pr, recovered densities are visible for the entire protein and confirm the dynamics of the upper domains, confirming the absence of compositional heterogeneity and a minimum of bias due to structural constraints. However, for Pfr, meaningful density of the upper (dynamic) part of the protein cannot be recovered, because the signal level in the averaged

density is too low. Thus, for this most dynamic protein case, volume-based debiasing is not possible,
 despite the fact that the structure based cryoSPHERE finds solutions that fit the data set.

6 DISCUSSION

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CryoSPHERE presents several advantages compared to other methods for volume and structure reconstruction.

Efficiency in Deformation: Deforming a base structure into a density map avoids the computationally expensive N_{pix}^2 evaluation required by a decoder neural network in methods implicitly parameterising the grid, such as Zhong et al. (2021a); Levy et al. (2022). Furthermore, direct deformation of a structure directly avoids the need for subsequent fitting into the recovered density map.

498 **Reduced Dimensionality and Noise Resilience:** Learning one rigid transformation per segment, 499 where the number of segments is much smaller than the number of residues, reduces the dimension-500 ality of the problem. This results in a smaller neural network size compared to approaches acting 501 on each residues, such as Rosenbaum et al. (2021). Rigidly moving large portions of the protein 502 corresponds to low-frequency movements, less prone to noise pollution than the high-frequency 503 movements associated with moving each residue independently. In addition, since our goal is to learn one rotation and one translation per segment, a latent variable of dimension $6 \times N_{\text{segm}}$ is, in 504 principle, a sufficiently flexible choice to model any transformation of the base structure. Choos-505 ing the latent dimension is more difficult for volume reconstruction methods such as (Zhong et al., 506 2021a). 507

Interpretability: CryoSPHERE outputs segments along with one rotation and one translation per
 segment, providing valuable and interpretable information. Practitioners can easily interpret how
 different parts are moving based on the transformations the network outputs. This interpretability is
 often challenging for deep learning models such as Zhong et al. (2021a); Rosenbaum et al. (2021).

512 Section 5 and Appendix B.2 demonstrate cryoSPHERE's capability to recover conformational het-513 erogeneity while performing structure reconstruction. The division into N_{segm} is learned from the 514 data and only marginally impacts the FSC to the ground truth. Moreover, cryoSPHERE recovers 515 the correct motion for the entire range of N_{segm} values and is able to keep the minimum necessary 516 number of domains when the user sets it too high (Appendix B.1).

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Structural restraints allow interpretation of low SNR datasets: It is evident that structural re-518 straints as implemented in cryoSPHERE (this work) and cryoSTAR provide additional restraints that 519 pure volume methods (i.e. cryoDRGN) lacks, thus giving better reconstructions for high noise data 520 sets. The additional restraints may introduce bias, which needs to be alleviated using a backprojec-521 tion algorithm. This, combined with cryoSPHERE's latent space, achieves better 0.5 cutoffs than 522 cryoDRGN, indicating its effectiveness in resolving conformational heterogeneity and debiasing the 523 results. If such a volume is unavailable, simply increasing N_{segm} can reduce the bias. As a note 524 of caution we find that for most dynamic protein studies here (the Pfr state of the phytochrome), 525 we find that volume-based debiasing fails because of the very low electron density levels in the 526 reconstructions. Here, other metrics should be developed in the future.

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Summary: Our study opens up for significant advancements in predicting protein ensembles and dynamics, critically important for unraveling the complexity of biological systems. By predicting all-atom structures from cryo-EM datasets through more realistic deformations, our work lays the foundation for extracting direct insights into thermodynamic and kinetic properties. This work is an important milestone in showing that one can learn a segmentation of the protein that is intimately linked to the change of conformation of the underlying protein, in an end-to-end fashion. In the future, we anticipate the ability to predict rare and high-energy intermediate states, along with their kinetics, a feat beyond the reach of conventional methods such as molecular dynamics simulations.

It would be interesting to assess how much our segmentation correlates with bottom-up segmentation into domains conducted on the "omics" scale, see e.g. Lau et al. (2023). To achieve this quantitatively, we would need many examples of moving segments from cryo-EM investigations to match the millions of segments from the "omics" studies. Therefore, we leave this investigation to later work.

5407REPRODUCIBILITY STATEMENT5417

As part of the current paper, we provide a github link to the source code in Section 1. We also describe in detail how we generate the synthetic datasets in Appendix B.2 and the hyperparameters chosen to run cryoStar, cryoSPHERE and cryoDRGN in Appendix B for each of the experiments.

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